



2. a.

$$\frac{d\psi}{dx} = A e^{-bx} - Abx e^{-bx}$$

$$\frac{d^2\psi}{dx^2} = -Ab e^{-bx} - Ab e^{-bx} + Ab^2 x e^{-bx}$$

$$-\frac{\hbar^2}{2m} [-2Ab e^{-bx} + Ab^2 x e^{-bx}] - \alpha/x A x e^{-bx} = E A x e^{-bx}$$

$$-\frac{\hbar^2}{2m} - 2Ab - \alpha A = 0$$

$$\Rightarrow \alpha = \frac{\hbar^2 b}{m} \Rightarrow \boxed{b = \frac{m\alpha}{\hbar^2}}$$

$$-\frac{\hbar^2}{2m} Ab^2 = E A$$

$$\Rightarrow E = -\frac{\hbar^2 b^2}{2m}$$

$$= -\frac{\hbar^2 m^2 \alpha^2}{2m \hbar^4}$$

$$= \boxed{-\frac{m\alpha^2}{2\hbar^2}}$$

b, $\int_0^\infty |\psi|^2 dx = 1$

$$\Rightarrow A^2 \int_0^\infty x^2 e^{-2bx} dx = 1$$

$$3. E_n = - \frac{m e^4}{32 \pi^2 \epsilon_0^2 \hbar^2} \cdot \frac{25}{n^2}$$

$$\Delta E_{12} = - \frac{m e^4}{32 \pi^2 \epsilon_0^2 \hbar^2} \cdot 25 \left(1 - \frac{1}{4}\right)$$

$$= \frac{hc}{\lambda}$$

$$\Rightarrow \lambda = \frac{hc \cdot 32 \pi^2 \epsilon_0^2 \hbar^2}{m e^4} \cdot \frac{4}{25}$$

$$= \frac{64 \pi^3 \epsilon_0^2 \hbar^3 c}{m e^4} \cdot \frac{4}{25}$$

4. $n \rightarrow$ Energy

$l \rightarrow$ Orbital Angular Momentum L

$m_l \rightarrow$ orientation of L

$m_s \rightarrow$ electron spin

$$5. \langle r \rangle = \int_0^{\infty} r \cdot r^2 \cdot \frac{4}{a_0^3} e^{-2r/a_0} dr$$

$$= \frac{4}{a_0^3} \int_0^{\infty} r^3 e^{-2r/a_0} dr$$

$$= \frac{4}{a_0^3} \cdot 3! / \left(\frac{2}{a_0}\right)^4$$

$$= \frac{4 \cdot 6 \cdot a_0}{16} = \frac{3a_0}{2}$$

6. $|A|^2$

