

Physics of Sound

Review

- I) Basic nature of physical science
 - A) Interaction of theory and experiment in constructing descriptions of structure.
 - B) Measurements and units. Variables and constants.
 - C) Equations and graphs as descriptions of relations. (linear, nonlinear, etc.)
- II) Simple Harmonic Motion (chapter 1).
 - A) Ingredients: inertia and linear restoring force.
 - B) Analogy to circular motion.
 - C) Damped and driven motion: resonance.
 - D) Force and motion: impedance, Newton's laws.
- III) Waves and Sound (chapter 2 also supplementary material).
 - A) Frequency, wavelength and speed. The spectrum.
 - 1) The speed of sound on strings, in solids, liquids, and in air.
 - B) Basic phenomena
 - 1) Linearity and "superposition".
 - a) Huygen's principle.
 - b) Interference: constructive and destructive.
 - c) Diffraction.
 - 2) Reflection.
 - a) Role of impedance.
 - b) "fixed" vs "free" end.
 - 3) Refraction
 - a) mirage
 - 4) Inverse square law (conservation of energy).
 - 5) Polarization
 - 6) Doppler shift (moving source, moving receiver).
 - 7) Shock wave.
 - C) Relation between velocity and pressure in sound– wave impedance.
- IV) Standing waves and overtones (Chapter 3).
 - A) Waves trapped by reflections: standing waves as the sum of two traveling waves.
 - B) Mersenne's Laws
 - C) Frequencies in the overtone series of strings and pipes.
 - D) "Intervals" and frequency ratios of overtones.
 - E) Modes and the analogy to simple harmonic motion. Resonance of modes.
 - F) Modes in higher dimension.
- V) Analysis and synthesis of complex waves (Chapter 4).
 - A) Representations of sound.
 - 1) Time domain $p(t)$.
 - 2) Frequency domain. $p(f)$
 - 3) Spectrogram $p(f,t)$; the compromise of resolving both.
 - B) Analysis of a complex sound in terms of the overtones.
 - C) Measures of tone quality
 - 1) Attack-decay transients.
 - 2) Inharmonicities.

- 3) Formants (filtering).
 - 4) Vibrato.
 - 5) Tremolo.
 - 6) Chorus effect.
- D) Resonance curves
 - E) Helmholtz oscillators.
- VI) Electronic music synthesis (chapter 5).
- A) Addition of waveforms.
 - B) Voltage controlled oscillators. Frequency Modulation (FM).
 - C) Voltage controlled amplifiers.
 - 1) Envelope generator
 - 2) Ring modulation (balanced modulation).
 - 3) Amplitude modulation (AM).
 - D) Voltage controlled filters (formants).
 - E) Noise generation.
 - F) Digital representation of sound.
- VII) The human ear and voice (chapter 6).
- A) Basic parts of the ear and vocal tract and their function.
 - B) Sound detection and the cochlea (place theory of hearing).
 - 1) Critical band.
 - 2) JND
 - C) Peculiarities of the ear.
 - 1) Ohm's law of hearing – little sensitivity to phase.
 - 2) Periodicity pitch and fundamental tracking.
 - 3) Masking.
 - 4) binaural effects (directionality)
 - 5) Combination tones.
 - 6) Amplitude and frequency response of the ear.
 - D) Linear (watts/m^2) and log (decibel) scales of Sound Intensity Level (SIL).
- VIII) Sound recording and reproduction (chapter 7 sections 1,3,4,and 10)
- A) The electro-mechanical analogy. Electrical force, motion, and impedance.
 - 1) Ohm's law of electricity $V=IR$.
 - 2) Electrical power. $P=VI$
 - B) Transducers
 - 1) Microphones of various types.
 - 2) Loudspeakers. and effects of the enclosure.
 - C) Digital representation.
- IX) Room and Auditorium Acoustics (chapter 8)
- A) Reverberation time (definition).
 - 1) How it is calculated.
 - B) Other terms: liveness, intimacy, fullness, clarity, warmth, brilliance, texture, blend, and ensemble.
 - C) The ray theory of sound.
 - D) Problems: focusing, echoes, shadows, resonances.
 - 1) Calculating room resonances.

- X) Basic acoustic components of musical instruments how: energy gets into sound.
 - A) Free energy->instability->/<-modes->filtering->radiation.
 - B) Types of instability.
- XI) Intervals, linear and log frequency axis. Circle of fifths.
- XII) Types of dynamics – linear vs nonlinear.

Some useful equations and numbers:
 Typical speed of sound in air: 340m/s

Vibration and waves in general: $T=1/f$ $\omega=2\pi f$

Waves in general: $f \cdot \lambda = S$

$$\text{Power: } P=Zv^2$$

$$\text{Sound in air: } S = \sqrt{\frac{\gamma RT}{M}} \approx (331.3 + 0.6 * T_{\text{celcius}}) \frac{m}{s}.$$

$$\text{Waves on strings: } S = \sqrt{\frac{F}{W}} \quad Z = \sqrt{F \cdot W} \quad W = \frac{M}{L}$$

$$\text{Simple harmonic oscillator: } \omega_{\text{res}} = 2\pi f_{\text{res}} = \sqrt{\frac{k}{m}}$$

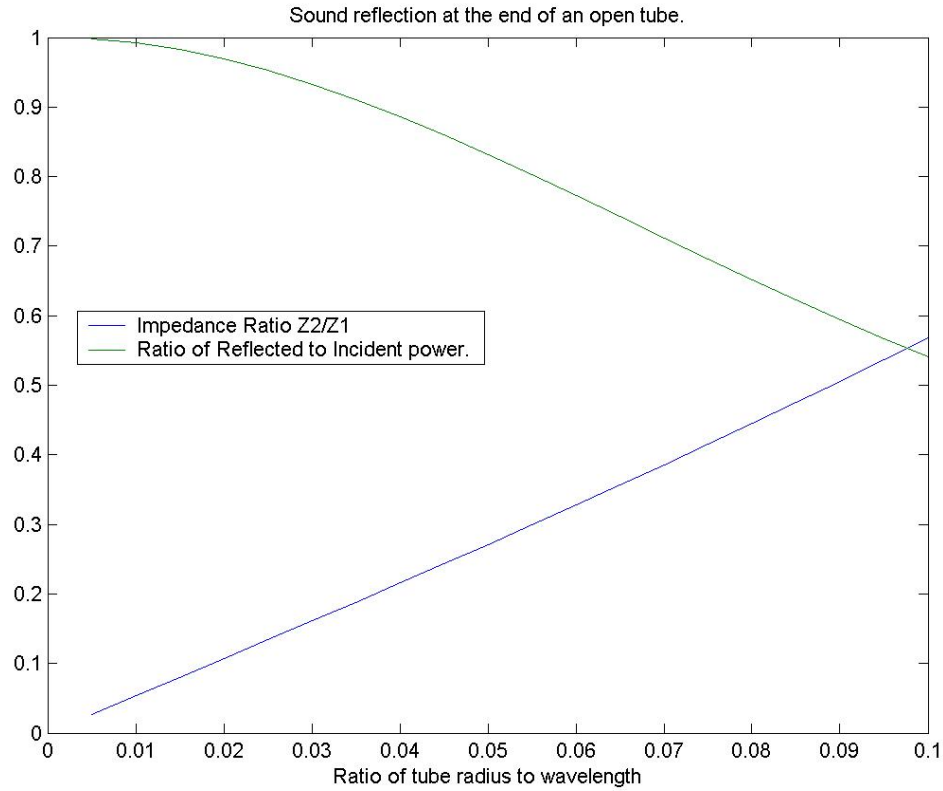
$$\text{Doppler effect (moving source): } \frac{f_{\text{source}}}{f_{\text{air}}} = 1 - \frac{v_s}{v}$$

$$\text{Doppler effect (moving receiver): } \frac{f_{\text{receiver}}}{f_{\text{air}}} = 1 + \frac{v_o}{v}$$

$$\text{Amplitude ratio of reflection from an impedance change: } \frac{A_r}{A_i} = \frac{1 - Z_2 / Z_1}{1 + Z_2 / Z_1}$$

Power ratio from an impedance change is the square of the amplitude ratio: $\frac{P_r}{P_i} = \left(\frac{A_r}{A_i}\right)^2$

$$\frac{r}{\lambda} = \frac{r}{S} \cdot f$$



Impedance of a tube.

$$Z_{tube} = \frac{Z_s}{A} = \frac{\sqrt{\gamma p n m}}{A} = \frac{n \sqrt{\gamma R T m}}{A} \quad \text{The units are Kg/(m}^4\text{s)}$$

Modes in strings and tubes with both ends the same.

$$f_1 = \frac{S}{2L}$$

$$T_1 = \frac{2L}{v}$$

$$f_n = n \cdot f_1 = n \cdot \frac{S}{2L}$$

$$f_1 = \frac{v}{2L} = \frac{1}{2L} \sqrt{\frac{F}{W}}$$

$$\lambda_n = \frac{2L}{n}$$

$$f_n = n \cdot f_1 = n \cdot \frac{v}{2L} = \frac{n}{2L} \sqrt{\frac{F}{W}} = \frac{1}{T_n}$$

$$L = n \frac{\lambda_n}{2}$$

Modes in tubes with one end open and one end closed.

$$f_1 = \frac{S}{4L}$$

$$f_n = n \cdot f_1; n = 1, 3, 5, 7, 9, \dots$$

$$\lambda_n = \frac{4L}{n}; n = 1, 3, 5, 7, 9, \dots$$

$$L = n \frac{\lambda_n}{4}; n = 1, 3, 5, 7, 9, \dots$$

Reverberation time

$$T_r = 55.2 \frac{V}{S \cdot A}$$

Electrical Ohm's law

$$V = I \cdot R \qquad P = V \cdot I = I^2 R = \frac{V^2}{R}$$

Log scale of sound intensity level.

$$SIL(db) = 10 \cdot \text{Log}_{10} \left(\frac{\text{Intensity}}{10^{-12} \text{ W / m}^2} \right) \qquad I = 10^{-12} \frac{\text{watts}}{\text{meter}^2} * 10^{\left(\frac{SIL(db)}{10} \right)}$$

$$SIL(db) = 20 \cdot \text{Log}_{10} \left(\frac{P_{RMS}}{2 \cdot 10^{-5} (\text{Pascal})} \right).$$

Modes in 3 dimensions (for modes in 2-d just set $N_z=0$)

$$f_{N_x, N_y, N_z} = \frac{S}{2} \sqrt{\left(\frac{N_x}{x} \right)^2 + \left(\frac{N_y}{y} \right)^2 + \left(\frac{N_z}{z} \right)^2}$$